

Hypothesis Testing 101

This page contains general information. For more information on what the hypotheses look like and how to calculate the test statistics, see the other documents.

Null Hypothesis:

- The claim that the sample observations happen by chance
- Usually a statement of “no change” or “no difference” (i.e. equals)
- Contains symbols about the population
- Denoted H_0

Alternative Hypothesis

- Our hypothesis, or what we want to prove
- Claim that we are trying to find evidence for
- Denoted H_a

*Information on concluding which is true the null or alternative hypothesis see below

Null Value: the value being tested

One-sided (one-tailed): when the alternative hypothesis states that the parameter is greater than, larger than, above, smaller than, less than, or below the null value

Two-sided (two-tailed): when the alternative hypothesis states that the parameter is not equal to or is different than the null value

Test Statistic:

- The calculated value of z, t, etc
- Measures how far the data deviates from what we expect

P-value:

- The probability (assuming H_0 is true) that the test statistic would take a value as extreme or more extreme than what was actually observed.
- Measures the strength of the support for the null hypothesis

Interpretation of p-value

Example: Interpret what p value of 0.04 means.

If H_0 was true, a sample as contrary to H_0 as our sample would occur by chance alone only 4% of the time if the experiment was repeated again and again.

In other words, a value as large as the statistic (e.g. sample mean, sample proportion) would only occur by chance in 4% of all samples when the null hypothesis is true.

Significance level:

- the level we compare our p-value to
- denoted α
- $\alpha=0.05$ (or 5%) unless stated otherwise
- probability of a type I error

Significance:

- does not mean important
- means not likely to happen by chance

Type I Error: Reject H_0 when H_0 is true

Type II Error: Fail to Reject H_0 when H_a is true

Power of the test: 1- probability of a type II error

Choosing the Null or Alternative Hypothesis**When the p-value is less than or equal to α**

- We *reject* the null hypothesis
- The data is statistically significant at the α level
- Significant Evidence for the alternative hypothesis

When the p-value is greater than α

- We *fail to reject* the null hypothesis
- The data is not statistically significant at the α level
- No evidence for the alternative hypothesis

For more information:

<http://www.stat trek.com/hypothesis-test/hypothesis-testing.aspx?Tutorial=Stat>

<http://www.stat trek.com/hypothesis-test/hypothesis-testing.aspx>

<http://www.statisticssolutions.com/resources/directory-of-statistical-analyses/hypothesis-testing>